Overview	Transition Systems	Example 1: mod-4 counter	Specifying properties in LTL	Example 2: Traffic light

Introduction to Model-Checking using Spin

Deepak D'Souza

Department of Computer Science and Automation Indian Institute of Science, Bangalore.

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Overview Transition S •0000 00

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Specifying properties in LT 00000000 Example 2: Traffic light 00000

Methods and tools covered in this course



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Model-checking using Spin: Plan of lectures

• Lecture 1 & 2: Intro to model-checking using Spin.

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• Lecture 3 & 4: How LTL model checking works.

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Outline of this lecture



- 2 Transition Systems
- 3 Example 1: mod-4 counter
- 4 Specifying properties in LTL
- 5 Example 2: Traffic light

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Overv	view of Spin			

Spin is a model-checking tool, in which we can

- Describe transition system models.
 - Suited for concurrent protocols, supports different synchronization constructs.
- Simulate them, explore paths in them.
- Describe desirable properties of the system in temporal logic.
- Check that the system satisfies these properties.
 - Proves that property is satisfied
 - Produces counter-examples (execution that violates property).

Overview	Transition Systems	Example 1: mod-4 counter	Specifying properties in LTL	Example 2: Traffic light
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Systems where Spin was successfully used

- Software control of Flood control barrier in The Netherlands. Verified the control algorithms.
- Call Processing logic of PathStar telephone switch: extraction of the model and verification of properties related to call-waiting/forwarding etc.
- Mission-Critical Software in Mars Rover and other space missions. Verification of resource (including motors) manager, hand-off protocols, etc.



More details at spinroot.com/spin/success.html. () ()

Overview	Transition Systems	Example 1: mod-4 counter	Specifying properties in LTL	Example 2: Traffic light
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Transition systems: states

A state (over a set of variables *Var* with associated types) is a valuation for the variables in *Var*.

Thus a state is a map $s: Var \rightarrow Values$, that assigns to each variable x a value s(x) in the domain of the type of x.

Example of a state

Consider $Var = \{loc, ctr\}$, with type of $loc = \{\texttt{sleep}, \texttt{try}, \texttt{crit}\}$, and type of $ctr = \mathbb{N}$. Example state s: $\langle loc \mapsto \texttt{sleep}, ctr \mapsto 2 \rangle$, depicted as:

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I ransition systems

A transition system is of the form $\mathcal{T} = (S, I, \rightarrow)$ where

- S is a set of states,
- $I \subseteq S$ is a set of initial states,
- $\rightarrow \subseteq S \times S$ is a transition relation.

A run or execution of \mathcal{T} is a (finite or infinite) sequence of states s_0, s_1, s_2, \ldots such that

- $s_0 \in I$, and
- for each $i, s_i \rightarrow s_{i+1}$.

Specifying properties in LTI

Example 2: Traffic light 00000

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Example transition system: a mod-4 counter

Transition system of a mod-4 counter

Here $Var = \{count\}$, with type of $count = \{0, 1, 2, 3\}$.

$$\begin{aligned} \mathcal{T} &= (S &= \{\langle count \mapsto 0 \rangle, \langle count \mapsto 1 \rangle, \langle count \mapsto 2 \rangle, \langle count \mapsto 3 \rangle \}, \\ I &= \{\langle count \mapsto 0 \rangle, \langle count \mapsto 1 \rangle \}, \\ \to &= \{(\langle count \mapsto 0 \rangle, \langle count \mapsto 1 \rangle), \\ (\langle count \mapsto 1 \rangle, \langle count \mapsto 2 \rangle), \\ (\langle count \mapsto 2 \rangle, \langle count \mapsto 3 \rangle), \\ (\langle count \mapsto 3 \rangle, \langle count \mapsto 0 \rangle) \}). \end{aligned}$$

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Example transition system: a mod-4 counter





Example run:



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Mod-4 counter in Spin

```
byte count = 0;
proctype counter() {
    do
    :: true -> count = (count + 1) % 4;
    od
}
init {
    run counter();
}
```



Property specifications in Temporal Logic

- Linear-time Temporal Logic (LTL) proposed by Amir Pnueli in 1978 to specify properties of program executions.
- What can we say in LTL? An LTL formula describes a property of an infinite sequence of "states."
 - *p*: an atomic proposition *p* (like "*count* = 2" or "*tick* = *false*") holds in the current state.
 - Xp ("next p"): property p holds in the tail of the sequence starting from the next state.
 - **F**p ("future p"): property p holds eventually at a future state.
 - *Gp* ("globally *p*"): property *p* holds henceforth (at all future states).
 - U(p,q) ("p Until q"): property q holds eventually and p holds till then.





Illustrating Semantics of an LTL formula

Example formula: $(count = 0 \lor count = 1) U (count = 2)$



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Syntax and semantics of LTL

Syntax:

$$\varphi ::= p \mid \neg \varphi \mid \varphi \lor \varphi \mid X\varphi \mid U(\varphi, \varphi).$$

Semantics: Given an infinite sequence of states $w = s_0 s_1 \cdots$, and a position $i \in \{0, 1, \ldots\}$, we define the relation $w, i \models \varphi$ inductively as follows:

$$\begin{array}{ll} w,i \models p & \text{iff} \quad p \text{ holds true in } s_i. \\ w,i \models \neg \varphi & \text{iff} \quad w,i \not\models \varphi. \\ w,i \models \varphi \lor \psi & \text{iff} \quad w,i \models \varphi \text{ or } w,i \models \psi. \\ w,i \models X\varphi & \text{iff} \quad w,i+1 \models \varphi. \\ w,i \models U(\varphi,\psi) & \text{iff} \quad \exists j: i \leq j, w,j \models \psi, \text{ and} \\ \forall k: i \leq k < j, w, k \models \varphi. \end{array}$$

 $F\varphi$ is shorthand for $U(true, \varphi)$, and $G\varphi$ is shorthand for $\neg(F\neg\varphi)$.

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Example 2: Traffic light 00000

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When a system model satisfies an LTL property

If \mathcal{T} is a transition system and φ is an LTL formula with propositions that refer to values of variables in \mathcal{T} , then we say $\mathcal{T} \models \varphi$ (read " \mathcal{T} satisfies φ ") iff each infinite execution of \mathcal{T} satisfies φ in its initial state.

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Example properties for counter model

```
byte count = 0;
proctype counter() {
  do
  :: true -> count = (count + 1) % 4:
 od
}
init {
  run counter();
3
ltl prop1 { [](count <= 3) };</pre>
ltl inc { []((count == 1) -> X(count == 2)) }
ltl prop3 { ((count == 0) || (count == 1)) U (count == 2));
ltl prop4 { [](count == 0) };
```

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Transition System generated by Spin

Extended transition system generated by Spin:



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Corresponding transition system:

Overview

Specifying properties in LTL 00000000

Example 2: Traffic light

Transition System generated by Spin: Example from Spin Primer and Ref book

```
Corresponding transition
                                                 system:
active proctype not_euclid(int x, y)
ſ
  if
  :: (x > y) \rightarrow L: x = x - y
  :: (x < y) \rightarrow y = y - x
                                                                   S_0
  :: (x == y) -> assert (x != y); goto L
                                                         x == v
  fi;
                                                               x > v
  printf(";%d\n", x)
                                                       S1
}
                                                           assert
                                                              x = x - y
                                                                   S<sub>4</sub>
```

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x < y

v = v-x

print Ss S_3

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Example with inputs: Traffic light model

"Stop" says the red light, "Go" says the green. "Change" says the amber light, blinking in between. That's what they say, and that's what they mean. We all must obey them, even the Queen!

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Traffic light model in Spin

```
mtvpe = { GREEN, AMBER, RED };
mtype = { GO, CHANGE, STOP };
bool tick = false:
mtype status = GO;
mtype light = GREEN;
byte ctr = 0:
active proctype TrafficLight() {
 do
  :: atomic {
     if
     :: tick = false;
     :: tick = true:
     fi;
     if
     :: (status == GD) && (ctr == 3) && tick -> status = CHANGE: ctr = 0:
     :: (status == CHANGE) && (ctr == 1) && tick -> status = STOP: ctr = 0:
     :: (status == STOP) && (ctr == 3) && tick -> status = CHANGE; ctr = 0;
     :: else -> ctr = (tick -> (ctr + 1) % 4 : ctr);
     fi:
     if
     :: status == GO -> light = GREEN;
     :: status == CHANGE -> light = AMBER;
     :: status == STOP -> light = RED;
     fi;
     3
 od:
3
ltl liveness { []((light == RED) -> <>(light == GREEN)) };
ltl sequence { []((light == RED) U ((light == AMBER) U (light == GREEN))) 9; → ( = > ( = > ) = → Q ( →
```

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Transition system for traffic light (partial)



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• Which of the properties below are true of the traffic light model?

G((light = red) => F(light = green));

G((light = red) U ((light = amber) U (light = green)));

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Exercise					

• Which of the properties below are true of the traffic light model?

G((light = red) => F(light = green));

G((light = red) U ((light = amber) U (light = green)));

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Pix model based on error trail found by Spin.

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Exerc	ise			

Which of the properties below are true of the traffic light model?

G((light = red) => F(light = green));

G((light = red) U ((light = amber) U (light = green)));

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- Pix model based on error trail found by Spin.
- Give modified properties that the system satisfies.

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Some example models

- Simple example modelling concurrency (race.pml, inc-dec-lock.pml)
- Example using channels for communication (prod-con.pml)

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• Example of post-facto use of Spin (Detecting races in FreeRTOS)

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Spin resources and other material

Spin webpage: http://spinroot.com/ Current version: Spin v6.5.1 Useful documentation:

- Spin documentation (tutorial, reference manual, etc): http://spinroot.com/spin/Man/.
- Material for other topics:
 - Textbook by Huth and Ryan, *Logic in Computer Science*: Specifications, semantics, and model-checking techniques for LTL.